

Functional limit theorem for moving average processes

(Talk)

Danijel Krizmanić
University of Rijeka, Croatia
dkrizmanic@math.uniri.hr

(joint work with Bojan Basrak and Johan Segers)

Functional limit theorems have been first obtained for independent and identically distributed random variables with finite second moments. We consider a strictly stationary sequence of random variables $(X_n)_{n \geq 1}$ with infinite second moments and show that under the properties of weak dependence and regular variation with index $\alpha \in (0, 2)$, the partial sum stochastic process

$$V_n(t) = a_n^{-1}(S_{[nt]} - [nt]b_n), \quad t \in [0, 1],$$

converges in distribution to an α -stable Lévy process in the space $D[0, 1]$ endowed with Skorohod's M_1 topology, where $S_n = X_1 + \dots + X_n$, (a_n) is a sequence of positive real numbers such that $nP(|X_1| > a_n) \rightarrow 1$ as $n \rightarrow \infty$, and $b_n = E(X_1 1_{\{|X_1| \leq a_n\}})$. Here, $D[0, 1]$ is the space of real-valued right continuous functions on $[0, 1]$ with left limits. The limiting process is characterized in terms of its characteristic triple. This result is then applied to moving average processes.

MSC2010: 60F17, 60G52.

Keywords: functional limit theorem, moving average, regular variation, mixing, stable processes.

Section: Probability and Statistics.