

# Lapidus zeta functions of fractal sets and applications

(Talk)

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(joint work with Michel L. Lapidus, University of California, Riverside, and Goran Radunović, University of Zagreb)

In 2009. Michel L. Lapidus has introduced a new class of zeta functions associated with bounded nonempty sets  $A$  in  $\mathbb{R}^N$ , defined by

$$\zeta_A(s) = \int_{A_\delta} d(x, A)^{s-N} dx,$$

where  $s$  is a complex number,  $A_\delta$  is the  $\delta$ -neighbourhood of  $A$ , and  $d(x, A)$  is the Euclidean distance from  $x$  to  $A$ . These zeta functions can serve as a bridge between the geometric theory of fractal sets and complex analysis. A special case are the classical Riemann zeta function and the zeta function of fractal strings. The abscissa of convergence of the Lapidus zeta function of  $A$  is equal to the upper box (or Minkowski) dimension of  $A$ . Furthermore, if  $A$  is Minkowski nondegenerate, then the upper and lower  $d$ -dimensional Minkowski contents of  $A$  are closely related to the value of the residue of the zeta function of  $A$  at  $s = d$ . We illustrate the properties of zeta functions of fractal sets in the case of generalized Cantor sets and geometric chirps. This is a continuation of previous studies of M. L. Lapidus and his collaborators on fractal strings and their generalizations over the past two decades.

## References

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